

# Announcements

MP5 av, due 10/30, 11:59p.

Exam 2: 11/3, 7-10p, in rooms TBA.

MP5soln party: 11/2, 6:30p

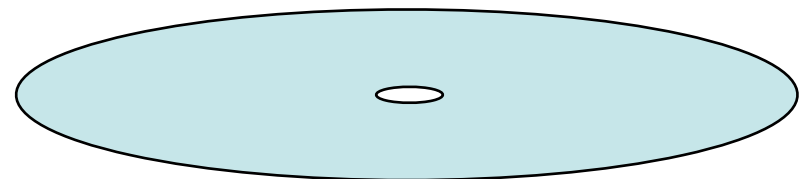
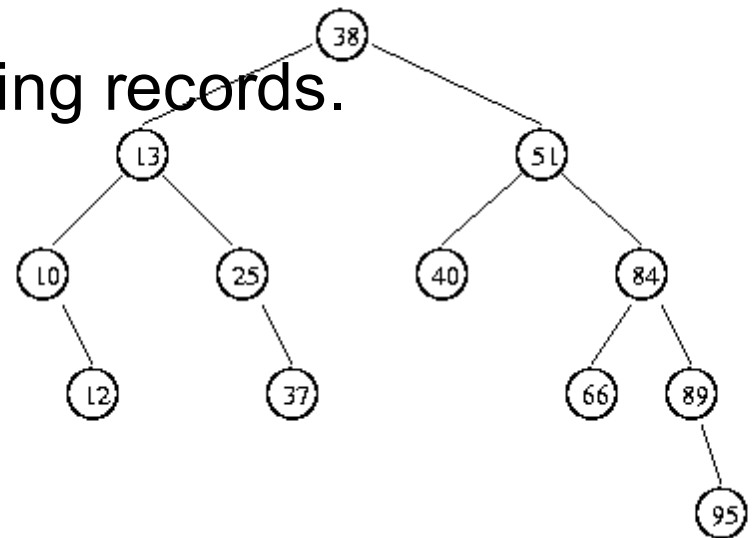
Review 11/1: 6:30p

Imagine an AVL tree storing US driving records.

How many records?

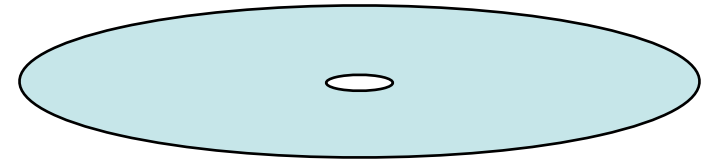
How deep is the AVL tree?

How many disk seeks to find a record?



# B Tree of order m

12	18	27	52	58	63	77	89
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Goal: Minimize the number of reads from disk

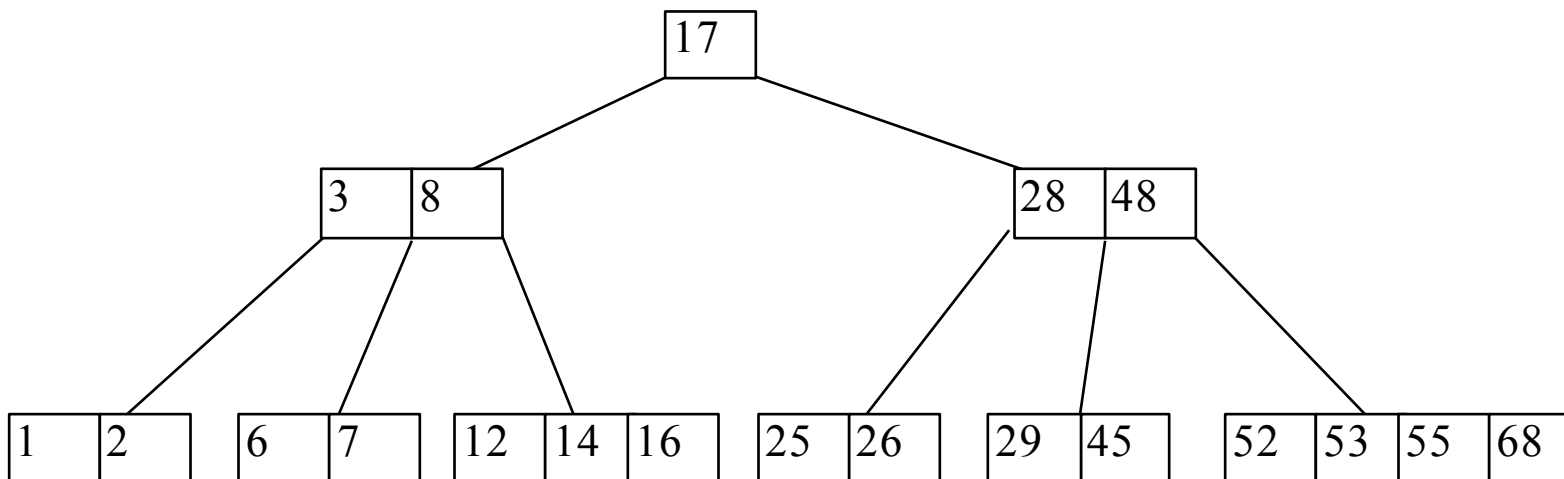
- Build a tree that uses 1 disk block per node
  - Disk block is the fundamental unit of transfer
- Nodes will have more than 1 key
- Tree should be balanced and shallow
  - In practice branching factors over 1000 often used

<http://people.ksp.sk/~kuko/bak/big/>

# Definition of a B-tree

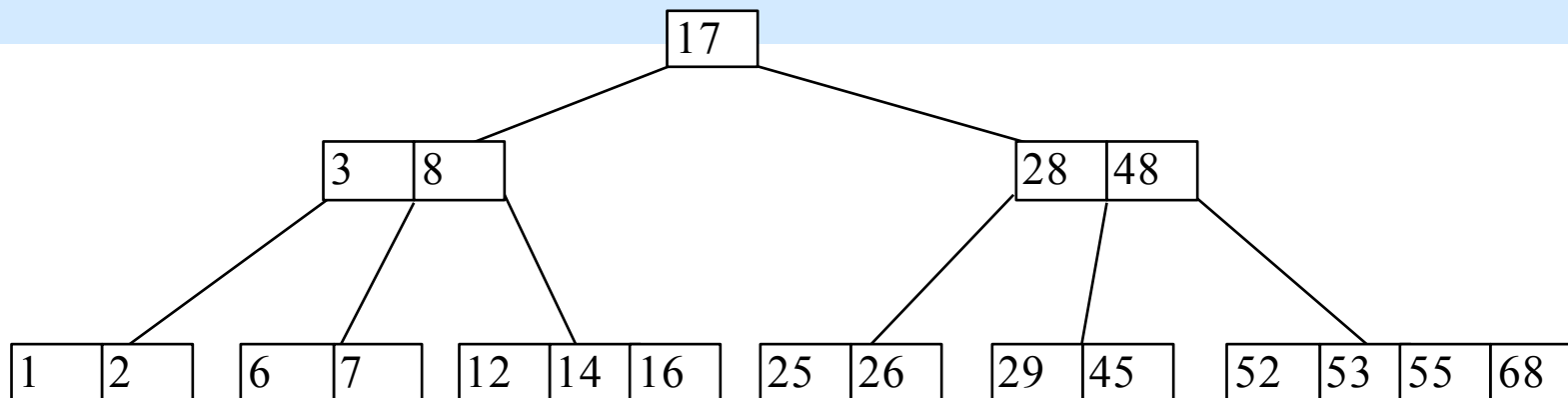
B-tree of order  $m$  is an  $m$ -way tree

- For an internal node, # keys = #children - 1
- All leaves are on the same level
- All leaves hold no more than  $m-1$  keys
- All non-root internal nodes have between  $\lceil m/2 \rceil$  and  $m$  children
- Root can be a leaf or have between 2 and  $m$  children.
- Keys in a node are ordered.



# Searching a B-tree

```
bool B-TREE-SEARCH(BtreeNode & x, T key){  
    int i = 0;  
    while ((i < x.numkeys) && (key > x.key[i]))  
        i++;  
    if ((i < x.numkeys) && (key == x.key[i]))  
        return true;  
    if (x.leaf == true)  
        return false;  
    else{  
        BtreeNode b=DISK-READ(x.child[i]);  
        return B-TREE-SEARCH(b, key);  
    }  
}
```



# Analysis of B-Trees (order $m$ )

The height of the B-tree determines the number of disk seeks possible in a search for data.

We want to be able to say that the height of the structure and thus the number of disk seeks is no more than \_\_\_\_\_.

As we saw in the case of AVL trees, finding an upper bound on the height (given  $n$ ) is the same as finding a lower bound on the number of keys (given  $h$ ).

We seek a relationship between the height of the structure ( $h$ ) and the amount of data it contains ( $n$ ).

# Analysis of B-Trees (order $m$ )

We seek a relationship between the height of the structure ( $h$ ) and the amount of data it contains ( $n$ ).

- The minimum number of *nodes* in each level of a B-tree of order  $m$ :  
(For your convenience, let  $t = \underline{\hspace{2cm}}$ .)

root

level 1

level 2

. . .

level  $h$

- The total number of nodes is the sum of these:

- So, the least **total** number of *keys* is:

# Analysis of B-Trees (order $m$ )

We seek a relationship between the height of the structure ( $h$ ) and the amount of data it contains ( $n$ ). (continued...)

- So, the least **total** number of *keys* is:
- rewrite as an inequality about  $n$ , the total number of keys:
- rewrite **that** as an inequality about  $h$ , the height of the tree (note that this bounds the number of disk seeks):

# Summary

## B-Tree search:

$O(m)$  time per node

$O(\log_m n)$  height implies  $O(m \log_m n)$  total time

BUT:

Insert and Delete have similar stories.

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## What you should know:

Motivation

Definition

Search algorithm and analysis

## What you should not know:

Insert and Delete